

Planet formation with different gas depleted timescales

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Outline

- Model
 - Sketch map
 - Results
 - Discussions
- 

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Model:

Surface density profile:

$$\text{MMSN: } \Sigma \propto r^{-3/2}$$

Conservation of mass:

$$\dot{M} = 2\pi R \Sigma \cdot (-v_R)$$

Conservation of angular momentum:

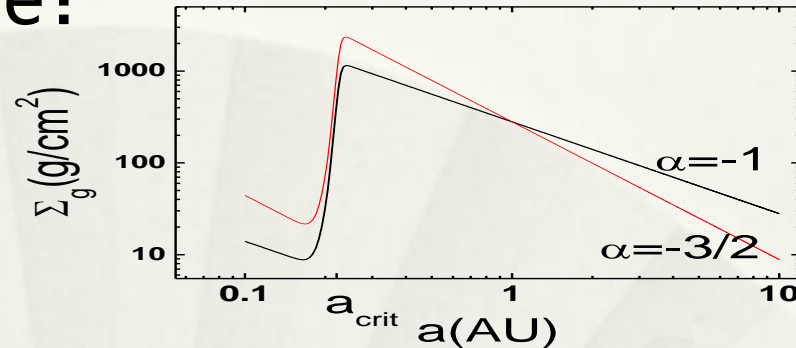
$$v \Sigma (-\Omega') = \Sigma (-v_R) \Omega - C / (2\pi R^3) \quad \Omega' = d\Omega / dR$$

$$R_* \Omega' = 0 \quad C = \dot{M} (G M R_*)^{1/2}$$

$$\Sigma = \frac{\dot{M}}{3\pi v} [1 - (R_* / R)^{1/2}] \quad (\text{Pringle, 1981})$$

$$v = \alpha c_s H, \quad c_s \propto H \Omega, \quad H \propto r^{5/4}$$

$$\Rightarrow \Sigma \propto r^{-1}$$



$$\Sigma_g = \Sigma_0 \text{ g cm}^{-2} f_g \left(\frac{\alpha_{\text{eff}}}{10^{-4}}\right) \left(\frac{M_*}{M_\odot}\right)^{-1/2} \left(\frac{a}{1\text{AU}}\right)^{-1} e^{-t/\tau_{\text{disk}}}$$

Considering MRI:

- ◆ Local maximum pressure
- ◆ Accumulation of embryos

General migrations:

Type I: *Cresswell & Nelson, 2006*

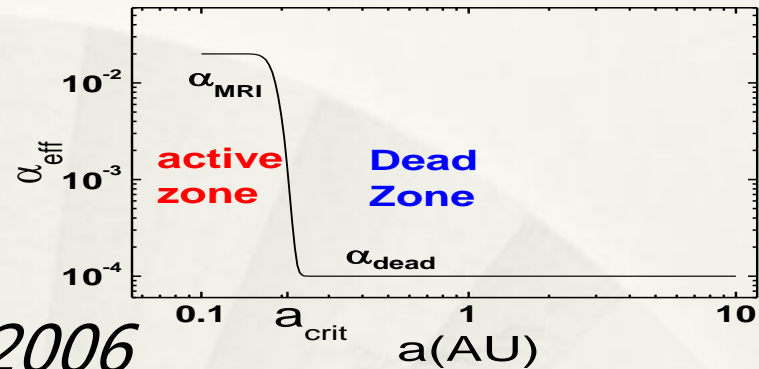
Type II: *Albert et al. 2005*

Tidal damp of gas disk

Cresswell & Nelson, 2006

different gas depleted timescales: 0.5–5Myr

Considering N-body interaction.



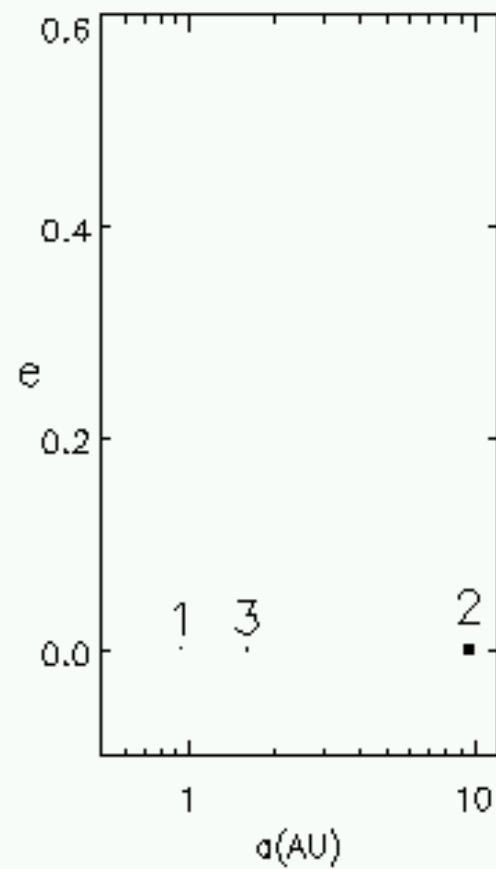
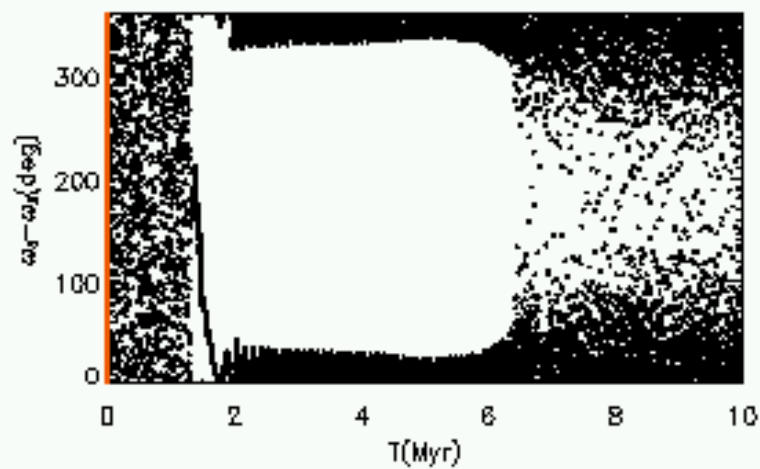
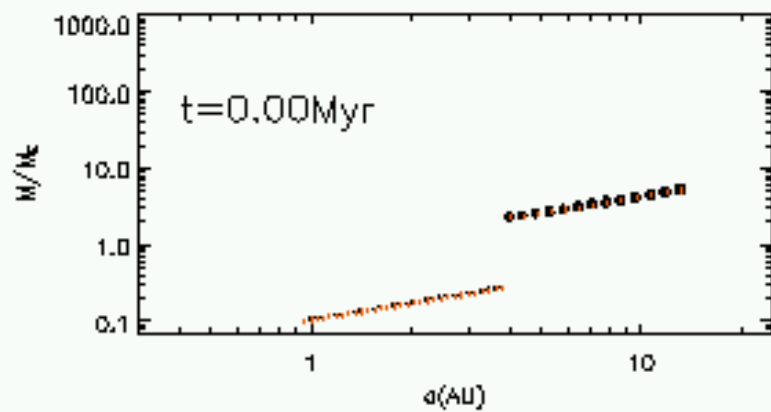
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Sketch map

- Collision growth
- Gas accretion (M_{crit})
 - long τ_{disk} : sufficient
 - small τ_{disk} : Insufficient
- Migration rate

An example of multi-planetary system:
44 embryos, 0.5~12 AU, Mass > 0.1 M_{E}



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Formation of planets with different sizes:

Giants

1-10AU

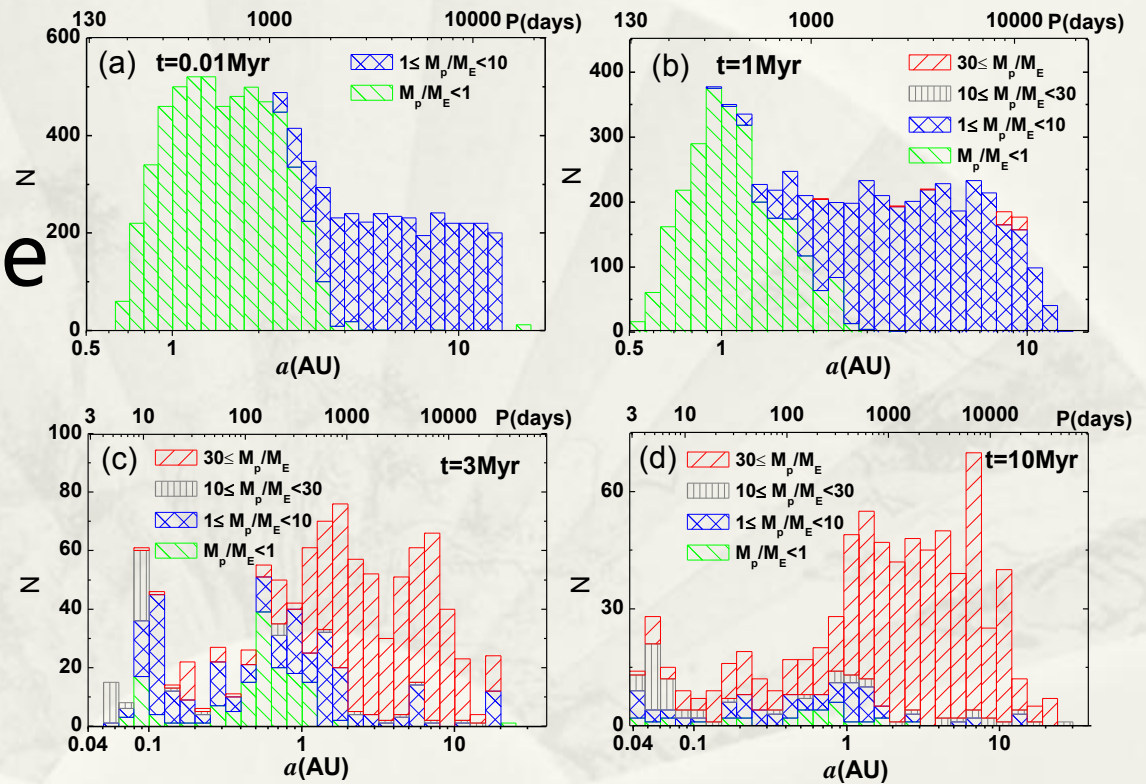
Neptune size

~ 0.05 AU

Super-Earth

Earth size

~ 1 AU



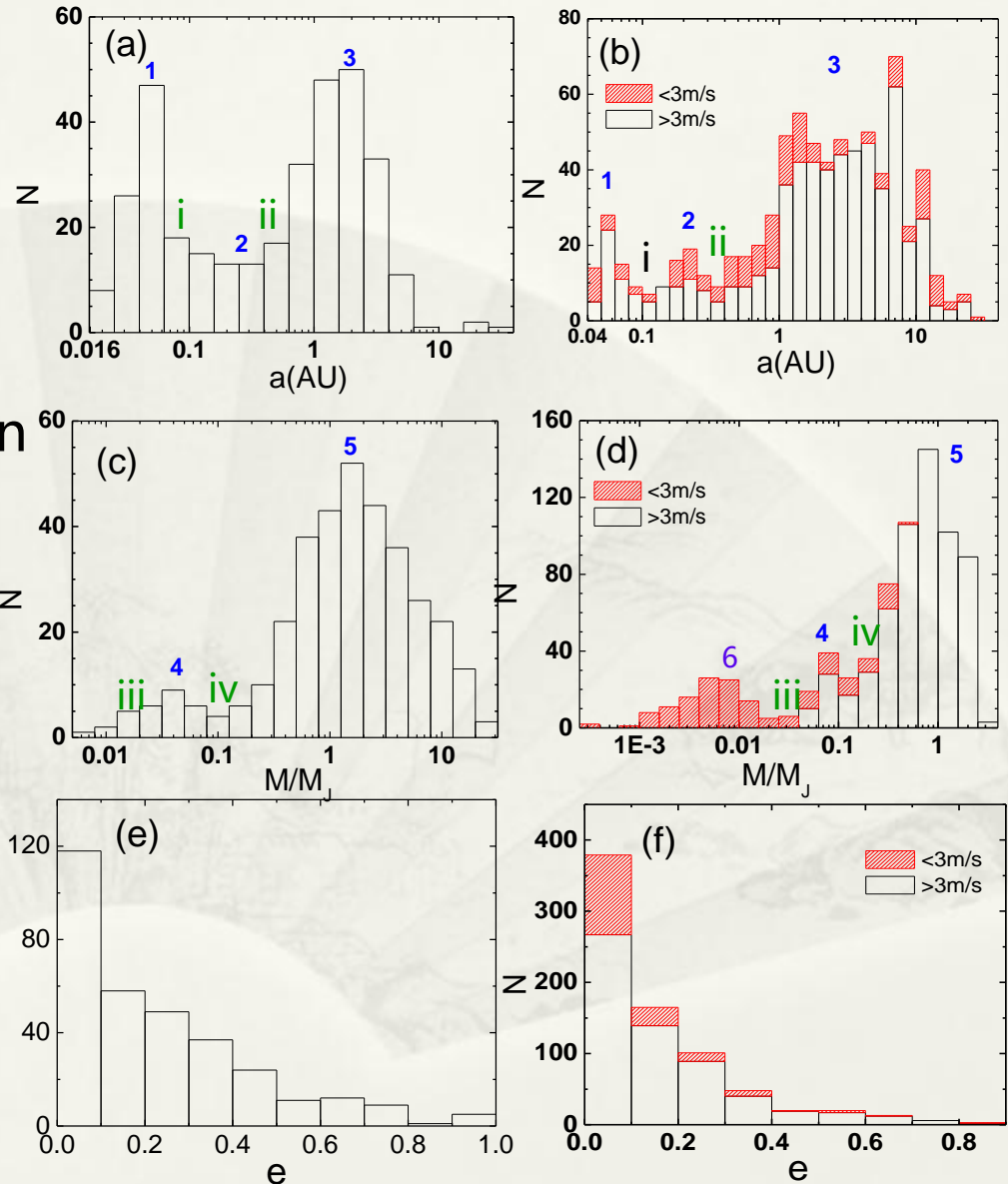
Peaks and deserts

Peaks:

- 1: inner boundary
- 2: MRI effect
- 3: Type II migration
- 4: insufficient gas accretion
- collision growth
- 5: Asymptotic Mass
- 6: Collision growth

Deserts:

- i, ii: MRI effect
- iii: onset of gas accretion
- iv: runaway gas accretion



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Discussion:

- Excluded effects:

Dynamical friction of small planetesimals

difficulty: time costing

Gravitation of gas disk.

tidal damp of host star

- Comparing with observations:

influence of $f_g, \dot{M}_{disk}, [Fe/H]$

- Uncertainty of initial conditions:

a, M of embryos.

The End

Thank You!

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